

Title:

**Unitary Correlations and the Fejer Kernel**

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Abstract:

Let  $M$  be a unitary matrix with eigenvalues  $t_j$ , and let  $f$  be a function on the unit circle. Define  $X_f(M) = \sum f(t_j)$ . We derive exact and asymptotic formulae for the covariance of  $X_f$  and  $X_g$  with respect to the measures  $|\chi(M)|^2 dM$  where  $dM$  is Haar measure and  $\chi$  an irreducible character. The asymptotic results include an analysis of the Fejer kernel which may be of independent interest.